

Aromaticity Evaluations of Planar [6]Radialenes

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Supporting Information

ABSTRACT: The aromatic character of fused polycyclic systems varies with the nature of their annulated rings. Computed extra cyclic resonance energies (ECREs) reveal that the central six membered rings (6MRs) of the heterocyclic fused congeners 1–5 are "[6]radialene-like", but that the central 6MRs of triphenylene 9, coronene 10, and isocoronene 11 are "benzene-like." Comparisons with geometric (harmonic oscillator model of aromaticity, HOMA) and magnetic (nucleus independent chemical shifts, NICS) criteria illustrate the multifaceted nature of aromaticity in 1–11.



The possible aromaticity of [6] radialene 1a and of its derivatives 1-5 (Figure 1) is intriguing because, like benzene, their central six-membered rings (6MRs) are comprised exclusively of sp²-hybridized carbons. Although the parent [6] radialene 1a is highly nonplanar, hetero-[6] radialenes 1b-c and the well-characterized 5MR annulated systems 2-5, are planar. The latter have often been used as π -electron acceptors in materials chemistry, but their aromaticity has not been systematically analyzed.

We now report a detailed study of the influence of the annulated rings and of the exocyclic C=C, C=O, and C=N

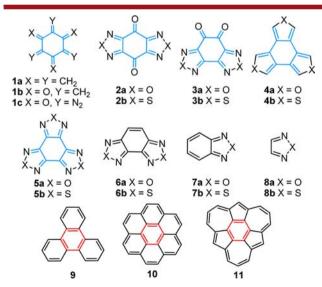


Figure 1. [6] Radialenes **1a-c**, polycyclic systems with planar [6] radialene cores **2-5**, heteroaromatics **6-8**, triphenylene **9**, coronene **10**, and isocoronene **11**.

bonds on the aromatic character of the central ring of planar $\lceil 6 \rceil$ radialenes 1–5 and of heteroaromatics 6–8. The results are compared with the aromaticity of the central 6MRs of triphenylene 9, coronene 10, and isocoronene 11 (Figure 1).6 Our analysis of the aromatic character of 1-11 is based on geometric (harmonic oscillator model of aromaticity HOMA), magnetic (nucleus-independent chemical shift, NICS),8 and energetic (extra cyclic resonance energy ECRE)9 criteria. All geometries were optimized at the B3LYP/6-31G(d) level employing Gaussian 03.10 For comparison, optimized geometries and calculated HOMA values for selected compounds were performed at the B3PW91/aug-cc-pVDZ level and included in the Supporting Information (SI). The HOMA index can be dissected into two independent contributions (eq 1) describing the effect of π -electron delocalization: EN, the mean bond length of a ring system, and GEO, the degree of ring bond length alternation.

$$HOMA = 1 - EN - GEO$$
 (1)

The HOMA, EN, and GEO parameters of benzene and 1-11 are listed in Table 1. Positive HOMA values indicate aromaticity; negative HOMAs indicate antiaromaticity or reduced aromatic character.

Notably, the benzene HOMA (+0.98) and the values for 1a-c have opposite signs. Although both benzene and [6] radialenes 1a-c have equalized ring CC bond lengths (GEO = 0), the mean ring CC lengths of 1a-c (up to 1.503 Å, large EN) are much longer than those of benzene (1.395 Å, EN \approx 0). The central rings of coronene 10 (+0.60) and isocoronene 11 (+0.84) are only somewhat less aromatic than that of benzene (+0.98), while the central ring of triphenylene 9 has significantly reduced aromatic character (+0.05).

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Table 1. Computed HOMA, EN, and GEO for Benzene, Planar [6]Radialenes 1a-c, and the Central 6MRs of the Polycyclic Systems 2-7 and 9-11

compound ^a	HOMA	EN	GEO
benzene ^b	0.98	0.021	0.000
1a (D_{6h})	-2.40^{c}	3.399	0.000
$1b^d$	-2.15	3.148	0.000
$1c^d$	-0.81	1.805	0.000
2a	-1.15	1.927	0.223
2b	-1.36	2.163	0.198
3a	-1.74	2.103	0.637
3b	-1.82	2.336	0.485
4a	-0.08	1.077	0.000
4b	-0.18	1.165	0.011
5a	0.18	0.807	0.010
5b	-0.10	1.097	0.007
6a	0.32	0.415	0.264
6b	0.19	0.519	0.290
7a	0.62	0.138	0.244
7 b	0.59	0.160	0.251
9	0.05	0.818	0.134
10	0.60	0.400	0.000
11	0.84	0.022	0.139
		. 1.	

^aHOMA(5MR) = +0.68 for 8a; see ref 7. ^bSee ref 6a. ^c-2.41 for nonplanar D_{3d} [6] radialene; ref 7c. ^dReference 2.

As shown in Figure 2, the 6MRs of 7a-b, 6a-b, and 5a-b display increasing "[6] radialene-character" and less positive

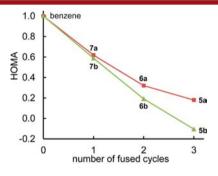


Figure 2. Changes in HOMA upon the annulation of benzene with one 7a-b, two 6a-b, and three 5a-b [1,2,5]-oxadiazole (red squares) or [1,2,5]-thiadiazole (green triangles) rings.

HOMA values when fused to one, two, and three heterocyclic 5MRs. Like benzene, the 6MRs of 5a-b (and the isoelectronic 4a-b) have nearly equal ring CC bond lengths (GEO \approx 0), but benzannulation elongates their mean lengths (up to 1.462~Å). However, increased ring bond alternation results when one of the 5MRs of 5a-b is replaced by two C=O bonds to give 3a-b. The CC bonds in the quinones, 2a-b and 3a-b, exhibit substantial elongation (up to 1.573~Å), and their 6MRs have large negative HOMA values, close to those of 1a-c. For comparison, the HOMA value for 1.4-benzoquinone (-0.83, two exocyclic C=O bonds) also is negative, indicative of substantially reduced aromatic character, or even of antiaromaticity. 12

The extra cyclic resonance energies (ECREs) were computed employing the block-localized wave function (BLW) method¹³ to quantify the aromatic stabilization energies associated with the "[6]radialene units" of 1–5 and the central 6MR of 9–11 (Table 2 and Figure 3). BLW-REs (REs, resonance energies) were evaluated by the computed energy difference between the fully

Table 2. Computed Dissected 6MR-NICS(0)_{πzz} (in ppm, at PW91/IGLOIII), BLW-REs (Adiabatic, at B3LYP/6-31G(d)), and 6MR-ECREs, for Benzene, for the 6MRs of 1–7 and 9–11 and for the 5MRs of 8a–b (See Text)

compound	$NICS(0)_{\pi zz}$	BLW-RE	6MR-ECRE
benzene	-36.9	61.39	+29.98
1a (D_{6h})	-1.2	54.28	-8.54
1b	+0.6	57.86	-3.94
2a	+4.4	129.27	+9.63
2b	+5.8	128.16	+12.22
3a	+4.6	131.99	+6.91
3b	+7.6	125.28	+9.34
4a	-22.8	195.70	-0.08
4b	-21.0	166.67	+2.90
5a	+3.6	175.61	+9.35
5b	+3.6	168.55	+11.92
6a	-7.2	128.62	+2.88
6b	-13.4	123.96	+4.64
7a	-24.9	87.93	+7.14
7b	-29.1	86.81	+9.23
8a	-28.7	47.82	+15.38
8b	-30.7	44.61	+18.33
9	-13.5	218.88	+34.71
10	-2.4	317.38	+28.54
11	-42.4	247.35	+43.23

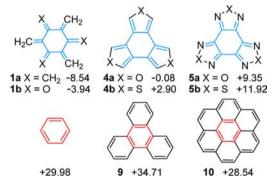


Figure 3. Computed 6MR-ECREs (in kcal/mol) for the central 6MRs of planar [6] radialenes **1**, **4**, **5** and for benzene, **9**, and **10**. The 6MRs being considered are highlighted in blue for "[6] radialene-like" and in red for "benzene-like" rings.

delocalized wave function (Ψ_{deloc}) of the molecule of interest and that of its hypothetical "localized" wave function (Ψ_{loc}), in which π -conjugations between each of the double bonds are mathematically "disabled" (BLW-RE = $\Psi_{loc} - \Psi_{deloc}$). ¹³

All 6MR-ECRE data were derived by the computed BLW-RE difference between that of the compound being considered minus that of the fused 5- or 6-MR(s) and π -conjugated units in the system (Table 2). For example, in coronene 10, the 6MR-ECRE for the central ring (+28.54 kcal/mol) is derived by the computed BLW-RE for 10 (317.38 kcal/mol) minus the BLW-REs of three benzene rings (61.39 × 3), six *anti*-butadienes (12.21 × 6), and three *syn*-butadienes (10.47 × 3). Based on this procedure, the computed 6MR-ECREs for 1–11 evaluate only the aromatic stabilization energy of the ring considered (Figure 3, central 6MR rings).

Six membered rings with large positive 6MR-ECRE values are aromatic and "benzene-like" whereas those with negative or close to zero 6MR-ECRE values are "[6]radialene-like." For reference, the computed ECRE for benzene is +29.98 kcal/mol, but that of

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planar [6] radialene, $\mathbf{1a}$ (D_{6h}), is -8.54 kcal/mol (note opposite sign). The ECRE of benzene is evaluated by its BLW-RE minus that of three *syn*-butadienes. The ECRE for $\mathbf{1a}$ is evaluated by the difference between its BLW-RE and that of six *syn*-butadienes. Direct comparisons of the computed 6MR-ECREs of $\mathbf{2}$ – $\mathbf{11}$ to those of benzene and of $\mathbf{1a}$ reveal the nature of the 6MR considered (Figure 3).

Remarkably, the type of ring annulation largely dictates the nature of the central 6MRs in 2-11. According to their 6MR-ECREs, the benzo-fused central rings of 9 (+34.71 kcal/mol) and 10 (+28.54 kcal/mol) are "benzene-like" (Figure 3, in red), but the heterocyclic 5MR-fused six-membered rings of 4-5 (6MR-ECREs ranging from -0.08 to +11.92) are weakly stabilized aromatically and display "[6] radialene-like" character (Figure 3, in blue). For comparison, the central 6-MR of isocoronene 11 is the most aromatically stabilized (+43.23 kcal/mol).6c-e Thus, despite also having three annulated rings, the 6MR-ECRE of 9 is three times larger compared to that of 5a-b (Figure 3). Changes in the number of fused rings may have less energetic impact. Thus, the 6MR-ECREs of 7a (+7.14 kcal/mol, one fused ring), 6a (+2.88 kcal/mol, two fused ring), and 5a (+9.35 kcal/mol, three fused ring) differ much less; all are within +10 kcal/mol (Table 2).

Comparisons of the energetic (6MR-ECRE) and the magnetic (dissected NICS_{$\pi / 2$}) criteria for the central ring of 9–11 and for the [6] radialene units of 1-7 elucidate the multifaceted nature of aromaticity in polycyclic systems. Dissected LMO^{8c} (localized molecular orbital)-NICS(0)_{πzz} values (at the PW91/IGLOIII level) were computed at the central ring of 1-11 to quantify their magnetic aromatic character (see Table 2). LMO-NICS distinguishes magnetic shielding contributions from each of the σ -bonds, π -bonds, and lone pairs. NICS_{$\pi z z z$} is the most refined NICS index for quantifying π -aromaticity, as it extracts the outof-plane tensor component of the isotropic NICS and includes contributions only from the π MOs. ^{8c} For monocyclic systems, aromatic rings have negative $\text{NICS}(0)_{\pi zz}$ values (diatropic) and antiaromatic rings have positive NICS(0)_{πzz} values (paratropic). However, in polycyclic systems, the interplay among multiple ring currents can lead to "artifactually" reduced diatropicity (e.g., in both the inner and outer 6MRs of 10, as discussed below) or enhanced paratropicity [e.g., in the central 6MRs of 2-5] for the individual rings examined.

In apparent agreement with Aihara, et al., 6f the computed $NICS(0)_{\pi zz}$ for both 9 and 10 suggest lower aromatic character for the central rings; but this is misleading (see below). The NICS behavior of the central rings in both 9 and 10 are influenced by the deshielding of the outer rings. Thus, 1a (-1.2)ppm), 1b (+0.6 ppm), and the central ring of coronene 10 (-2.4ppm) all have NICS(0)_{πzz} values close to zero (Table 1), but their 6MR-ECREs differ drastically (-8.54, -3.94, and +28.54 kcal/ mol, respectively). The monocyclic planar [6] radialenes 1a-b are nevertheless nonaromatic, but the central ring of 10 is almost as aromatic as benzene (see ECREs in Figure 3). In 10, the magnetic aromaticity of the central ring is lowered "artifactually," as it resides in the joint deshielded region of six (outer) aromatic rings. In contrast, the diatropicities of each of the outer 6MRs of 10 $(NICS(0)_{\pi zz} = -17.0 \text{ ppm}, \text{ Figure 4})$ maintain half of the aromatic character of benzene, as they reside in the deshielding regions of only three neighboring aromatic rings. In 9, the corresponding inner (-13.5 ppm, three adjacent aromatic rings)and outer (-36.1 ppm, one adjacent aromatic ring, bottom right)six-membered rings have more negative $NICS(0)_{\pi \gamma \gamma}$ values (Figure 4), since they are deshielded by fewer adjacent aromatic

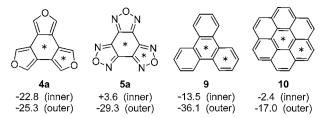


Figure 4. Computed NICS(0)_{$\pi z z$} values (in ppm, at PW91/IGLOIII) at the individual ring centers (NICS point indicated by black star) of **4a**, **5a**, and **9–10**.

rings. In isocoronene 11, the central 6-MR (NICS(0)_{πzz} = -42.4 ppm) as well as outer 5-MRs (NICS(0)_{πzz} = -38.6 ppm) and 7-MRs (NICS(0)_{πzz} = -53.5 ppm) are all highly aromatic, due to a peripheral ring current. ⁶

The more negative NICS(0)_{πzz} values of the 6MRs of 4a (-22.8 ppm) vs 5a (+3.6 ppm) also are the result of the more deshielded central 6MR in 5a (Figure 4). Since N's are more electronegative than C's, the N-containing 5MRs (NICS(0)_{πzz} = -29.3 ppm) of 5a competes more effectively for π -aromaticity and deshields the central 6MR (+3.6 ppm). In 4a, both the outer (5MR, -22.8 ppm) and inner (6MR, -25.3 ppm) rings are nearly equally aromatic. Thus, the 6MR of 5a is magnetically more "[6]radialene-like" while that of 4a is more "benzene-like."

Likewise, the sequential annulation of benzene (NICS(0) $_{\pi zz}$ = -36.9 ppm) with one 7a-b (6MR-NICS(0) $_{\pi zz}$ = -24.9, -29.1 ppm), two 6a-b (-7.2, -13.4 ppm), and three 5a-b (+3.6, +3.6 ppm) 5MRs result in increasingly less negative NICS(0) $_{\pi zz}$ values, since the 6MRs become increasingly *deshielded* (see Table 1). For the same reason, the central rings of 2a-b and 3a-b have positive 6MR-NICS(0) $_{\pi zz}$ values (+4.4 to +7.6 ppm, Table 2) but are not antiaromatic (cf. positive 6MR-ECRE values ranging from +6.9 to +12.2 kcal/mol, Table 2).

Depending on the nature of their annulated rings, fused benzenoids can have either "benzene-like" (aromatic) or "[6]radialene-like" (nonaromatic) character. As the aromatic character of polycyclic systems is multifaceted, aromaticity evaluations based on geometric, magnetic, and energetic criteria do not always agree, but provide complementary insights. 15

ASSOCIATED CONTENT

Supporting Information

Cartesian coordinates and energies for all optimized species. This material is available free of charge via the Internet at http://pubs. acs.org.

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Notes

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